

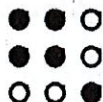
4.11 Graphs & Characteristics of Polynomials

Engage: Polynomial Patterns

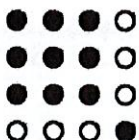
$n = 1$



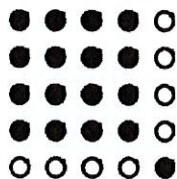
$n = 2$



$n = 3$



$n = 4$



a) For the diagram to the left, what do you notice and wonder?

Answers will vary.

b) Describe how you see the number of black dots changing or the number of white dots changing. Choose one color to focus on.

Black dots

n	1	2	3	4
# of dots	2	5	10	17

increase by consecutive odd #'s each time starting with 3

White dots

n	1	2	3	4
# of dots	2	4	6	8

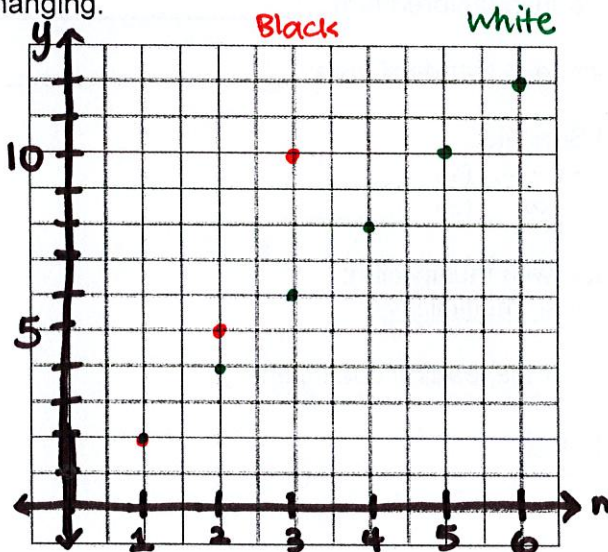
increase by 2

c) Write an equation to model how the dots are changing for the color you chose in part b).

Black : $y = n^2 + 1$

White : $y = 2n$

d) Create a graph to model how the dots are changing.



e) How could the graph be useful?

f) What is a real-life scenario that these images might be representing?

Answers will vary.

Explore: Puzzling over Polynomials

Learning Focus: Combine pieces of information about polynomials to write equations and graph them. Identify features of polynomials from equations and graphs.

Each of these polynomial puzzles given contain a few pieces of information. Your job is to use that information to complete the puzzle. Occasionally, you may find a missing piece that you can fill in yourself. For instance, although some of the roots are given, you may decide that there are others that you can fill in. When you need to graph a function, imagine what it will look like before using technology. Then use technology to graph the function and see how close your idea was to the actual function.

As you are working through the problem, pause and reflect after each one to answer the question: **What are the characteristics of the function that you knew from just the equation that was given?**

1)

Function in factored form: $f(x) = 2(x-1)(x+3)^2$

End Behavior:

As $x \rightarrow -\infty, f(x) \rightarrow -\infty$

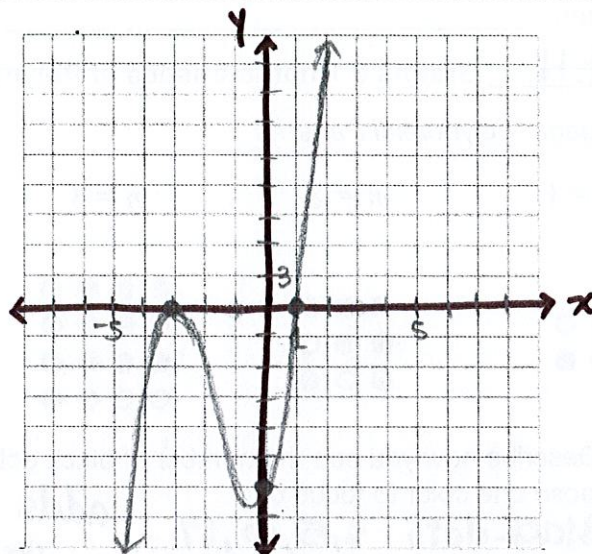
As $x \rightarrow \infty, f(x) \rightarrow \infty$

Roots (with multiplicity):

1, -3 w/mult. 2

Value of the leading coefficient: 2

Domain: all real #'s Range: all real numbers
 $(-\infty, \infty)$ $(-\infty, \infty)$



2)

Function in factored form: $f(x) = -2(x+2)(x-1)^2$

Function in standard form: $f(x) = -2x^3 + 6x - 4$

End Behavior:

As $x \rightarrow -\infty, f(x) \rightarrow \infty$

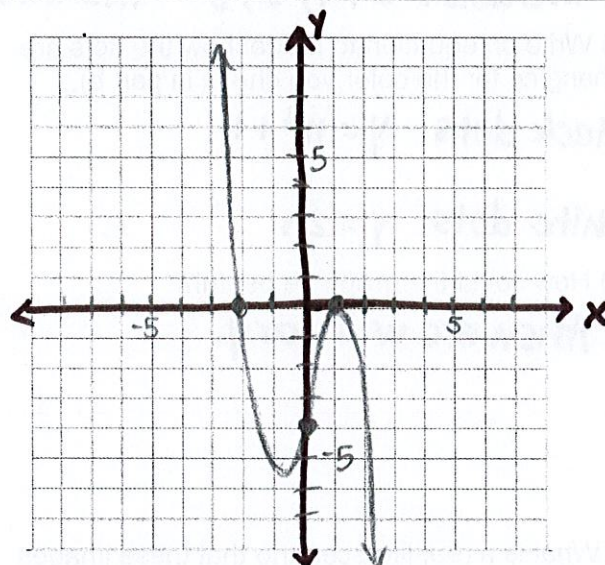
As $x \rightarrow \infty, f(x) \rightarrow -\infty$

Roots (with multiplicity):

-2, 1 with multiplicity 2

Value of the leading coefficient: -2

Degree: 3



3)

Function in factored form: $f(x) = -x^2(x-3)(x+1)^2$

Function in standard form: $f(x) = -x^5 + x^4 + 5x^3 + 3x^2$

End Behavior:

As $x \rightarrow -\infty, f(x) \rightarrow \infty$

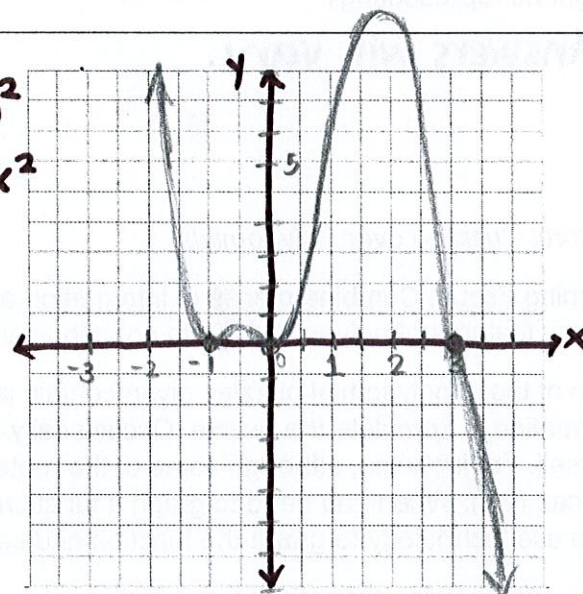
As $x \rightarrow \infty, f(x) \rightarrow -\infty$

Roots (with multiplicity):


3, -1 with multiplicity 2, 0 with multiplicity 2

Value of the leading coefficient: -1

Domain: all real #'s Range: all real #'s
 $(-\infty, \infty)$ $(-\infty, \infty)$



Graphs & Characteristics of Polynomials

① $f(x) = 2x^3 + \dots$ ← 1ST TERM POS & ODD 

$$f(0) = 2(-1)(3)^2 = -18 \leftarrow y\text{-intercept}$$

② $f(x) = -2(x+2)(x-1)^2$ ← factored form
PST


$$f(x) = -2(x+2)(x^2 - 2x + 1)$$

$$f(x) = -2(x^3 - 2x^2 + x + 2x^2 - 4x + 2)$$

$$f(x) = -2(x^3 - 3x + 2)$$

$$f(x) = -2x^3 + 6x - 4$$

$$f(0) = -2(0)^3 + 6(0) - 4 = -4 \leftarrow y\text{-intercept}$$

1ST TERM: $-2x^3$ NEG & ODD 

③ $f(x) = -x^2(x-3)(x+1)^2$ ← factored form
PST

$$f(x) = -x^2(x-3)(x^2 + 2x + 1)$$

$$= -x^2(x^3 + 2x^2 + x - 3x^2 - 6x - 3)$$

$$= -x^2(x^3 - x^2 - 5x - 3)$$

$$f(x) = -x^5 + x^4 + 5x^3 + 3x^2 \leftarrow \text{standard form}$$

1ST TERM: $-x^5$ NEG & ODD 