

## 2.1 Intercepts, Maximums and Minimums

### A: Intercepts

#### Algebraically

To find x-intercept, set y or f(x) equal to zero and then solve for x.

$$(x, 0)$$

Ex: Find the x-intercept of the function  $4x + 3y = 27$

$$4x + 3(0) = 27$$

$$\frac{4x}{4} = \frac{27}{4}$$

$$x = \frac{27}{4}$$

point

$$\left(\frac{27}{4}, 0\right)$$

To find y-intercept, set x equal to zero and evaluate/solve for y.

$$(0, y)$$

Ex: Find the y-intercept of the function  $f(x) = 3 + 2^x$

$$y = 3 + 2^x$$

$$y = 3 + 2^0$$

$$y = 3 + 1$$

$$y = 4$$

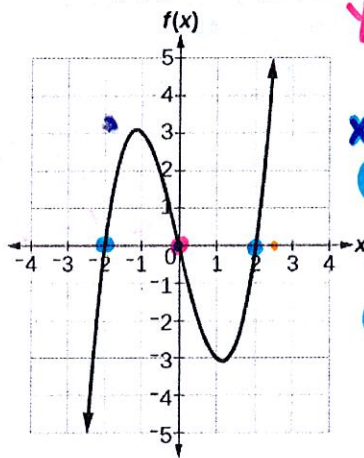
point

$$(0, 4)$$

#### Graphically

x-intercept: where the graph touches/crosses the x-axis

Ex: Find the x-intercept(s) on the graph.



y-int:  $(0, 0)$

x-int(s):

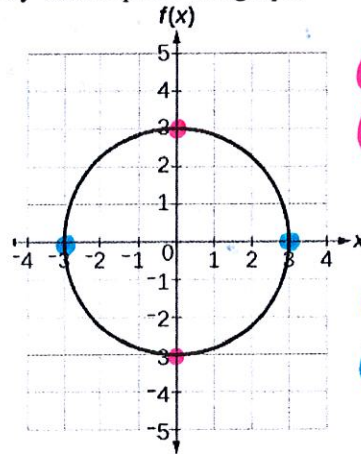
$$(-2, 0)$$

$$(2, 0)$$

$$(0, 0)$$

y-intercept: where the graph touches/crosses the y-axis

Ex: Find the y-intercept on the graph.



y-int:  $(0, 3)$

$(0, -3)$

x-int(s):

$$(-3, 0)$$

$$(3, 0)$$

*If an intercept falls between 2 values on the number line, estimate that intercept using a decimal value.*

**Round decimals to nearest tenth.**

**(1 decimal place)**

Find all of the intercepts for the functions below:

1.  $f(x) = 2 - x$

x-int:  $(2, 0)$  y-int:  $(0, 2)$

2.  $f(x) = \frac{x-2}{3}$

x-int:  $(2, 0)$  y-int:  $(0, -\frac{2}{3})$

3.  $f(x) = x^2 + 1$

4.  $f(x) = 4 - x^2$

5.  $f(x) = 2$

6.  $f(x) = x^3$

7.  $f(x) = x(x-1)(x+2)$

8.  $f(x) = \sqrt{x-2}$

9.  $f(x) = \sqrt{5-x}$

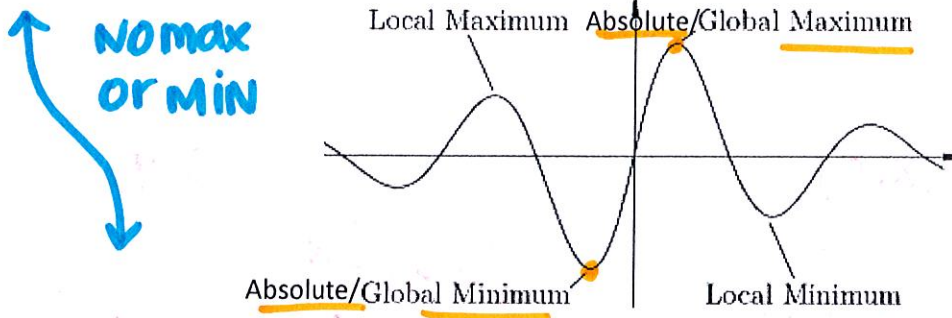
10.  $f(x) = 3 - 2\sqrt{x+2}$

11.  $f(x) = \sqrt[3]{x}$

12.  $f(x) = \frac{1}{x^2+1}$

## B: Maximums and Minimums

Remember maximums are hills and minimums are valleys.



You will not learn an algebraic way to find maximums and minimums, you must use the graph or graphing calculator to find the maximums and minimums of the graph.

<p>Ex: Identify the maximums and minimums on the graph below.</p>	<p>Ex: Identify the maximums and minimums on the graph below.</p>
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Use the calculator to find the maximums and minimums of the functions below. If the function has no maximum or no minimum, please note that.

1.  $y = x^3 - 5x^2 + 7x - 5$     **MAX (1, -2)**    2.  $y = x^3 - 6x^2 + 9x + 1$

**MIN (2.3, -3.2)**

3.  $y = -x^3 - 3x^2 - 1$

4.  $y = 3x^2 - 6x + 5$

5.  $y = 5 - |x - 4|$

6.  $y = (2x - 8)^{\frac{2}{3}}$

7.  $y = -x^2 + 6$

8.  $y = \sqrt{x - 3} + 2$



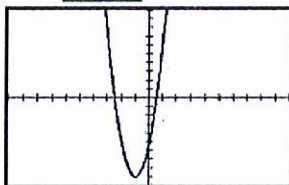
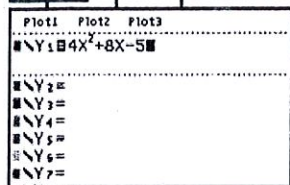
## 2.1 Calculator Instructions For Finding Intercepts(Zeros), Maximums and Minimums

### To Find X-intercepts/Zeros

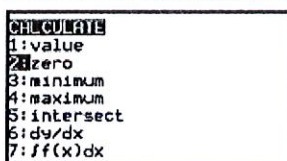
Method 1:

**Step 1:** Click on **ON**. Click on **Y=**.

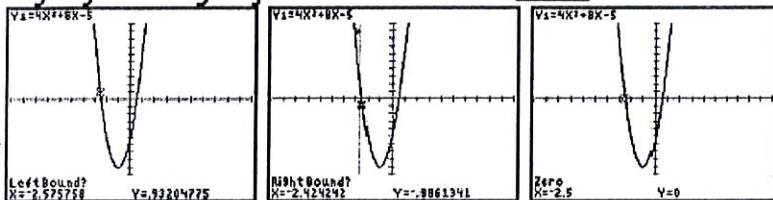
**Step 2:** Input equation into  $Y_1=$ . Click **GRAPH**.



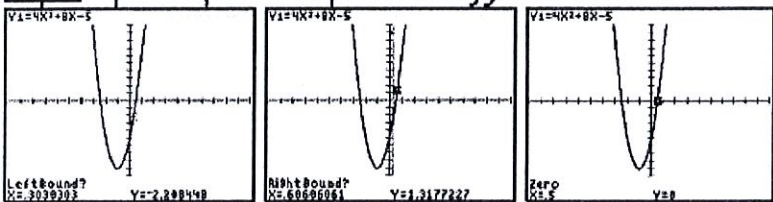
**Step 3:** Click on **2nd** → **TRACE**.  
 Choose **2: zero**.



**Step 4:** Move the blinking dot slightly to the left of one of the zeros by using the **←** or **→**. Click **ENTER**. Move the dashed line slightly to the right of the same zero. Click **ENTER** twice.



**Step 5:** Repeat Step 3 and Step 4 to identify the other zero.



### To Find y-intercept

Method 1:

Click on **Y =**

Input equation into  $Y_1 =$

Click **2nd**, **TRACE**

Choose **1: value**

Press "0"

Method 2:

Click on **Y =**

Input equation into  $Y_1 =$

Set  $Y_2 = 0$

Click **GRAPH**

Click **2nd**, **TRACE**

Choose **5: intersect**

Move blinking dot close to the x-intercept you want to find by using left and right arrows. Click **ENTER** three times.

Your intersection point is the x-intercept.

Method 2:


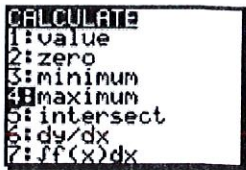
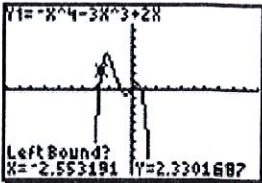
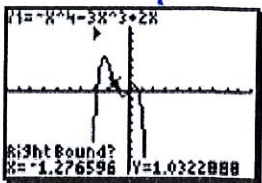
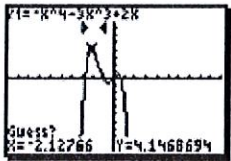
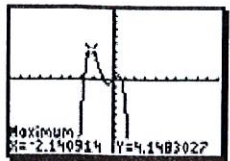
Click on **Y =**

Input equation into  $Y_1 =$

Click **2nd**, **GRAPH**

Look at the output for  $x = 0$

To Find Maximums and Minimums

PROBLEM	BUTTONS	CALCULATOR
<p>Locate the <b>maximum</b> of the Function:</p> $y = -x^4 - 3x^3 + 2x$	<p>1. First graph the function</p> <p><math>Y=</math> , <math>(-)</math> , <math>X,T,\theta,n</math> , <math>^{\wedge}</math> , <math>4</math> , <math>-</math> , <math>3</math> , <math>X,T,\theta,n</math> , <math>^{\wedge}</math> , <math>3</math> , <math>+</math> , <math>2</math> , <math>X,T,\theta,n</math> , <math>ZOOM</math> , <math>6</math></p> <p>2. Press, <math>2^{nd}</math> , <math>TRACE</math> , <math>4</math></p> <p>3. Using the <i>LEFT</i> arrow key , <math>\leftarrow</math> , move the cursor to the left of the maximum point and press <math>ENTER</math> .</p> <p>4. Using the <i>Right</i> arrow key , <math>\rightarrow</math> , move the cursor to the right of the maximum point and press <math>ENTER</math> .</p> <p>5. Finally, using the arrow keys , <math>\leftarrow</math> , <math>\rightarrow</math> , move the cursor to the approximate location of the maximum point and press <math>ENTER</math> .</p> <p>(-2.14 , 4.15)</p>	     
<p>Locate the <b>minimum</b> of the Function:</p> $y = x^2 - 5x$	<p>Using a very similar technique try locating the minimum. Just use the <i>MINIMUM</i> command under the <i>CALCULATE</i> window.</p>	