Date:	Period:
to 4?	_
to x?	_
de length equal to $x +$ the area of the base o	
the area of the base b	by the height $(x + 4)$ and
l to <i>x</i> + <i>y</i> ? Use the sar	ne steps as in Step 3 to
	to 4? to x? de length equal to <i>x</i> + the area of the base o the area of the base b

7. Determine whether the cube of a binomial is equivalent to the sum of two cubes by exploring the following expressions:

a. Simplify $(x + 2)^3$. b. Simplify $x^2 + 2^3$

c. Is your answer to part a equivalent to your answer in part b?_____

d. Simplify
$$(x + 2)(x^2 - 2x + 4)$$

polynomial identities:

e. Is your answer to part b equivalent to your answer in part d?

f. Your answers to part b and d should be equivalent. They illustrate two more commonly used

The Sum of Cubes (SOC): $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$ The Difference of Cubes (DOC): $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$

	Difference of Cube	es (DOC)	S	teps & Notes	Sum of Cubes (SOC)
	$a^3 - b^3 = (a - b)(a^2 - b)$				$a^{3} + b^{3} = (a + b)(a^{2} - ab + b^{2})$
	1. $x^3 - 8$	Perfect	Cube	1) Factor out the	3. $27x^3 + 1$
		Cube	Root	GCF, if any.	
		1	1	2) Find the cube	
		8	2	root of the first term	
		27	3	and the cube root of the last term.	
		64	4		
	2. $2000x^3 - 686$	125	5	2) Substitute cube	4. $512x^3 + 125y^3$
	2. $2000\lambda = 000$	216	6	roots into the formulas to the left.	4. $512x + 125y$
		343	7	Pay attention to the	
		512	8	signs. SOP.	
10		729	9	Be sure to simplify the squares, if	
2 Terms		1000	10	necessary.	
L		1000	10]	
Le Le					
N					
	Difference of	of Squares	s (DOS) and Sum of Sq	uares (SOS) Revisited
	$a^{2} - b^{2} = (a + b)(a - b)$				
	$\mathbf{a}^2 + \mathbf{b}^2 = (\mathbf{a} + \mathbf{b}\mathbf{i})(\mathbf{a} - \mathbf{b}\mathbf{i})$				
	5. $3x^4 - 3$			to Use: Look for	6. $36x^4 - 25y^2$
			perfect squares minus or plus perfect squares.		
			Remember variables with		
				exponents are all	
			perfec	t squares.	
			Alway	s check for GCF 1 st .	
			D		
				reful using the sum of es formula: this is	
				for quadratic	
				ssions.	
		2n -		ratic Form (QF)	n)
	7 4 4 2 4 7	ax ² " +		$\frac{\mathbf{c} = (\mathbf{m}\mathbf{x}^{\mathbf{n}} - \mathbf{p})(\mathbf{k})}{\mathbf{t} = \mathbf{k} \mathbf{s} \mathbf{s} \mathbf{s}^{\mathbf{n}} \mathbf$	1/
	7. $x^4 - 4x^2 - 45$			to Use : A polynomial ssion that has three	9. $2x^6 - x^3 - 15$
			terms,	one of the terms is a	
				ant and one exponent times the other	
			expon		
			-		
S			Alway	s check for GCF 1 st .	
3 Terms			Factor	the expression as if	
ē	8. $2x^4 + 34x^2 + 140$			a quadratic but then	10. $2x^8 - 3x^4 - 35$
				sure that you have	
				rrect variable ent in the	
				theses.	

	four terms and the degree is 3 or higher. There must be some proportionality between the pairs of terms.		$a^{3} + 3a^{2}b + 3ab^{2} + b^{3} = (a + b)^{3}$ $a^{3} - 3a^{2}b + 3ab^{2} - b^{3} = (a - b)^{3}$		
4 Terms	11. Factor $x^3 - 2x^2 + 5x - 10$	Grouping 1) Group the first two terms and the last two terms. 2) Factor the GCF out of both pairs.	13. Factor $x^3 - 15x^2 + 75x - 125$		
	12. Factor $x^3 + 2x^2 - 9x - 18$	3) The binomial in the parentheses should match and will be one factor and the common factors together make the second binomial.	14. Factor $8x^3 + 36x^2 + 54x + 27$		
		4) If one of the factors can be factored further, keep factoring until complete.			
		Binomial Cubed 1) Find the cube roots of the first and last terms.			
		2) Determine if the formula holds for the middle term.			
		 Make a binomial of the cube roots and cube it. 			
Notes: If the 2 nd and 4 th terms have opposite signs, you will need to factor out a negative GCF from the second pair of terms.					
not m	binomials in the parentheses in Step 3 do atch then check your GCFs or this ssion cannot be factored by grouping.				