$\qquad$ Date: $\qquad$ Period: $\qquad$

## Factoring Polynomials (3+ Degree)

## Engage: Cubic Identities

1. What is the volume of a cube with side length equal to 4 ? $\qquad$
2. What is the volume of a cube with side length equal to $x$ ? $\qquad$
3. Now we will determine the volume of a cube with side length equal to $x+4$.
a. First, use the rule for squaring a sum to find the area of the base of the cube.
b. Now use the distributive property to multiply the area of the base by the height $(x+4)$ and simplify your answer.
4. What is the volume of a cube with side length equal to $x+y$ ? Use the same steps as in Step 3 to determine this.
5. So the identify for a binomial cube is: $(x+y)^{3}=$ $\qquad$
6. Determine the following identity: $\quad(x-y)^{3}=$ $\qquad$
Explain or show how you came up with your answer.
7. Determine whether the cube of a binomial is equivalent to the sum of two cubes by exploring the following expressions:
a. Simplify $(x+2)^{3}$.
b. Simplify $x^{2}+2^{3}$
c. Is your answer to part a equivalent to your answer in part b? $\qquad$
d. Simplify $(x+2)\left(x^{2}-2 x+4\right)$
e. Is your answer to part b equivalent to your answer in part d? $\qquad$
f. Your answers to part b and d should be equivalent. They illustrate two more commonly used polynomial identities:

The Sum of Cubes (SOC):
The Difference of Cubes (DOC):
$a^{3}+b^{3}=(a+b)\left(a^{2}-a b+b^{2}\right)$
$a^{3}-b^{3}=(a-b)\left(a^{2}+a b+b^{2}\right)$

|  | Difference of Cubes (DOC)$a^{3}-b^{3}=(a-b)\left(a^{2}+a b+b^{2}\right)$ |  | Steps \& Notes |  | $\begin{gathered} \text { Sum of Cubes (SOC) } \\ a^{3}+b^{3}=(a+b)\left(a^{2}-a b+b^{2}\right) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1. $x^{3}-8$ <br> 2. $2000 x^{3}-686$ | Perfect | Cube | 1) Factor out the GCF, if any. <br> 2) Find the cube root of the first term and the cube root of the last term. <br> 2) Substitute cube roots into the formulas to the left. Pay attention to the signs. SOP. Be sure to simplify the squares, if necessary. | 3. $27 x^{3}+1$ <br> 4. $512 x^{3}+125 y^{3}$ |
|  |  | 1 | 1 |  |  |
|  |  | 8 | 2 |  |  |
|  |  | 27 | 3 |  |  |
|  |  | 64 | 4 |  |  |
|  |  | 125 | 5 |  |  |
|  |  | 216 | 6 |  |  |
|  |  | 343 | 7 |  |  |
|  |  | 512 | 8 |  |  |
|  |  | 729 | 9 |  |  |
|  |  | 1000 | 10 |  |  |
|  | Difference of Squares (DOS) and Sum of Squares (SOS) Revisited$\begin{gathered} \mathbf{a}^{2}-\mathbf{b}^{2}=(\mathbf{a}+\mathbf{b})(\mathbf{a}-\mathbf{b}) \\ \mathbf{a}^{2}+\mathbf{b}^{2}=(\mathbf{a}+\mathbf{b i})(\mathbf{a}-\mathbf{b i}) \end{gathered}$ |  |  |  |  |
|  | 5. $3 x^{4}-3$ |  | When perfec plus $p$ Reme even perfec Alway <br> Be car squar strictly expre | to Use: Look for squares minus or erfect squares. mber variables with exponents are all squares. <br> check for GCF $1^{\text {st }}$. <br> reful using the sum of formula: this is for quadratic ssions. | 6. $36 x^{4}-25 y^{2}$ |
|  | Quadratic Form (QF)$\mathbf{a x}^{2 \mathbf{n}}+\mathbf{b} \mathbf{x}^{\mathbf{n}}+\mathbf{c}=\left(\mathbf{m x ^ { n }}-\mathbf{p}\right)\left(\mathbf{k} x^{\mathbf{n}}-\mathbf{q}\right)$ |  |  |  |  |
| $\begin{gathered} \text { © } \\ \underset{\sim}{E} \\ \end{gathered}$ | 7. $x^{4}-4 x^{2}-45$ 8. $2 x^{4}+34 x^{2}+140$ |  | When expre terms, consta it two expon <br> Alway <br> Facto it were make the co expon paren | to Use: A polynomial sion that has three one of the terms is a ant and one exponent times the other ent. <br> check for GCF $1^{\text {st }}$. <br> the expression as if a quadratic but then sure that you have rrect variable ent in the theses. | 9. $2 x^{6}-x^{3}-15$ 10. $2 x^{8}-3 x^{4}-35$ |



