

1.4

Radicals

Simplify

Multiply

Divide

Rationalize the Denominator

Add & Subtract

Use factor tree or birthday cake to find prime factorization. Find pairs so they can come out.

1 Simplify $\sqrt{32}$

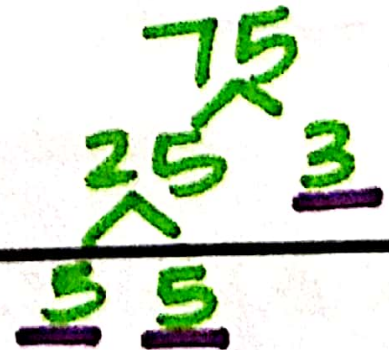
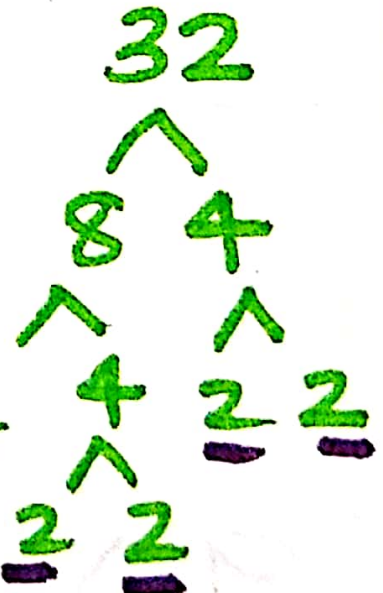
$$\sqrt{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2}$$

$$2 \cdot 2 \sqrt{2} = 4\sqrt{2}$$

2 Simplify $\sqrt{75x^3}$

$$\sqrt{3 \cdot 5 \cdot 5 \cdot x \cdot x \cdot x}$$

$$5x \sqrt{3x}$$



Simplify

Product Property

Algebra:

$$\sqrt{ab} = \sqrt{a} \cdot \sqrt{b}$$

Examples:

$$\begin{aligned} \textcircled{3} \quad \sqrt{9} \cdot \sqrt{9} &= \sqrt{9 \cdot 9} \\ &= \sqrt{81} \\ &= 9 \end{aligned}$$

$$\begin{aligned} \textcircled{4} \quad 3\sqrt{g} \cdot \sqrt{2g^3} &= 3\sqrt{2 \cdot \underbrace{g \cdot g \cdot g}_{\text{green}} \cdot \underbrace{g}_{\text{orange}}} \\ 3\sqrt{g \cdot 2g^3} &\rightarrow 3\sqrt{2 \cdot \underbrace{g \cdot g \cdot g}_{\text{green}} \cdot \underbrace{g}_{\text{orange}}} \\ 3\sqrt{2g^4} &= 3g \cdot \underbrace{g}_{\text{orange}} \sqrt{2} = \boxed{3g^2\sqrt{2}} \end{aligned}$$

$$\textcircled{5} \quad 2\sqrt{mn^2} \cdot \sqrt{5m^2}$$

$$2\sqrt{5n^2m^3}$$

$$2\sqrt{5 \cdot \underbrace{n \cdot n}_{\text{green}} \cdot \underbrace{m \cdot m \cdot m}_{\text{orange}}}$$

$$\boxed{2nm\sqrt{5m}}$$

Multiply

Quotient Property

Algebra:

$$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$$

Examples:

$$\textcircled{6} \sqrt{\frac{5}{49}} = \frac{\sqrt{5}}{\sqrt{49}} = \frac{\sqrt{5}}{7}$$

$$\begin{array}{c} 49 \\ \wedge \\ 7 \quad 7 \end{array}$$

$$\begin{aligned} \textcircled{7} \sqrt{\frac{11}{d^4}} &= \frac{\sqrt{11}}{\sqrt{d^4}} = \frac{\sqrt{11}}{\sqrt{d \cdot d \cdot d \cdot d}} \\ &= \frac{\sqrt{11}}{d \cdot d} = \frac{\sqrt{11}}{d^2} \end{aligned}$$

Divide

NO RADICALS CAN BE LEFT IN THE DENOMINATOR!

Multiply by the radicand in the denominator to the top & bottom.

Note: $\frac{\sqrt{7}}{\sqrt{7}} = 1$

Examples:

8 $\frac{7}{\sqrt{6}} \cdot \frac{\sqrt{6}}{\sqrt{6}} = \frac{7\sqrt{6}}{6}$

$\frac{\sqrt{6} \cdot \sqrt{6}}{\sqrt{36}}$
6

9 $\frac{\sqrt{3}}{\sqrt{5a}} \cdot \frac{\sqrt{5a}}{\sqrt{5a}} = \frac{\sqrt{15a}}{5a}$

$\frac{\sqrt{5a} \cdot \sqrt{5a}}{\sqrt{25a^2}}$
5a

Rationalize the Denominator

LIKE RADICALS have
the same # under
the radical.

Add/subtract the
coefficients to
combine like radicals.

* Make sure all
radicals are
simplified.

Examples:

⑩ $7\sqrt{14} + \sqrt{21} - 4\sqrt{14}$

$3\sqrt{14} + \sqrt{21}$

$$\begin{array}{r} 14 \\ \wedge \\ 7 \ 2 \\ \hline \end{array}$$

$$\begin{array}{r} 21 \\ \wedge \\ 7 \ 3 \\ \hline \end{array}$$

⑪ $5\sqrt{7} + \sqrt{28}$

$5\sqrt{7} + \sqrt{2 \cdot 2 \cdot 7}$

$5\sqrt{7} + 2\sqrt{7}$

$7\sqrt{7}$

$$\begin{array}{r} 28 \\ \wedge \\ 7 \ 4 \\ \hline \wedge \\ 2 \ 2 \\ \hline \end{array}$$

Add & Subtract